

**DEPARTMENT OF ECONOMICS
UNIVERSITY OF CYPRUS**



**THRET: THRESHOLD REGRESSION WITH ENDOGENEOUS
THRESHOLD VARIABLES**

Andros Kourtellos, Thanasis Stengos and Chih Ming Tan

Discussion Paper 2008-03

P.O. Box 20537, 1678 Nicosia, CYPRUS Tel.: ++357-2-892430, Fax: ++357-2-892432
Web site: <http://www.econ.ucy.ac.cy>

THRET: Threshold Regression with Endogenous Threshold Variables

Andros Kourtellos
Department of Economics
University of Cyprus*

Thanasis Stengos
Department of Economics
University of Guelph[†]

Chih Ming Tan
Department of Economics
Tufts University[‡]

First Draft: June 2006

This Draft: November 13, 2007

Abstract

This paper extends the simple threshold regression framework of Hansen (2000) and Caner and Hansen (2004) to allow for endogeneity of the threshold variable. We develop a concentrated two-stage least squares (C2SLS) estimator of the threshold parameter that is based on an inverse Mills ratio bias correction. Our method also allows for the endogeneity of the slope variables. We show that our estimator is consistent and investigate its performance using a Monte Carlo simulation that indicates the applicability of the method in finite samples. We also illustrate its usefulness with an empirical example from economic growth.

JEL Classifications: C13, C51

*P.O. Box 537, CY 1678 Nicosia, Cyprus, e-mail: andros@ucy.ac.cy.

[†]Guelph, Ontario N1G 2W1, Canada, email: tstengos@uoguelph.ca

[‡]8 Upper Campus Road, Medford, MA 02155, email: chihming.tan@tufts.edu.

1 Introduction

One of the most interesting forms of nonlinear regression models with wide applications in economics is the threshold regression model. The attractiveness of this model stems from the fact that it treats the sample split value (threshold parameter) as unknown. That is, it internally sorts the data, on the basis of some threshold determinants, into groups of observations each of which obeys the same model. While threshold regression is parsimonious it also allows for increased flexibility in functional form and at the same time is not as susceptible to curse of dimensionality problems as nonparametric methods.

While there are several econometric studies on the statistical inference of this model, there is as yet no available inference when the threshold variable itself is endogenous. Chan (1993) showed that the asymptotic distribution of the threshold estimate is a functional of a compound Poisson process. This distribution is too complicated for inference as it depends on nuisance parameters. Hansen (2000) using a concentrated least squares (TR-CLS) approach developed a more useful asymptotic distribution theory for both the threshold parameter estimate and the regression slope coefficients under the assumption that the threshold effect becomes smaller as the sample increases. Using a similar set of assumptions, Caner and Hansen (2004) studied the case of endogeneity in the slope variables. They proposed a concentrated two stage least squares estimator (IVTR-C2SLS) for the threshold parameter and a GMM estimator for the slope parameters. Gonzalo and Wolf (2005) proposed subsampling to conduct inference in the context of threshold autoregressive models. Seo and Linton (2005) allow the threshold variable to be a linear index of observed variables and propose a smoothed least squares estimation strategy based on smoothing the objective function in the sense of Horowitz's smoothed maximum scored estimator. They show that their estimator exhibits asymptotic normality but it depends on the choice of bandwidth.

In all these studies a crucial assumption is that the threshold variable is exogenous. It turns out, however, that in economics many threshold variables depend on their dynamics. In this paper we introduce the Threshold Regression with Endogenous Threshold variables (THRET) and the Threshold Regression with both Endogenous Threshold and Slope variables (THRETS) models and propose an estimation strategy that extends Hansen (2000) and Caner and Hansen (2004). First of all, we show that the naive concentrated 2SLS estimator is an inconsistent estimator of the threshold parameter. Instead, we propose concentrated two-stage least squares estimation (C2SLS) procedure by augmenting the threshold regression with the inverse Mills ratio which resembles the Heckman's selection correction. Under similar assumption as in Caner and Hansen (2004) we show that our estimators are consistent. Our estimation method also allows for endogeneity in the slope variables. To examine the finite sample properties of our estimators we provide a thorough Monte Carlo analysis that shows that for different sample sizes and parameter combinations our proposed

estimators for the threshold parameter and the slope coefficients are relatively more efficient than their existing competitors and their distributions have the correct means.

We consider an application of our estimation strategy to a problem that formed our original motivation for thinking about THRET models. We revisit in Section 5 of the paper one of the most important and ongoing debates in the growth empirics literature: the “institutions vs. geography” debate. The key question in this debate is whether geography has direct effects on long-run economic performance or if its influence is limited only to its effects on other growth determinants, such as institutions. Attempts to resolve this debate have centered on the use of linear cross-country regressions where the dependent variable is purchasing-power parity adjusted GDP per capita in 1995 while proxies for institutional quality, climate, disease ecology, macroeconomic policies, and endowments form the set of regressors.

Acemoglu, Johnson, and Robinson (2001), Easterly and Levine (2003), and Rodrik, Subramanian, and Trebbi (2004) conclude that geography’s influence on long-run income levels is solely indirect through its effects on institutions, while Sachs (2003) argues that their conclusions are wrong once a measure of malaria transmission is included. Sachs goes further by suggesting that the search for mono-causal effects of fundamental growth determinants on growth may be misdirected. He concludes that, “[t]here is good theoretical and empirical reason to believe that the development process reflects a complex interaction of institutions, policies, and geography [Sachs (2003), p. 9].”

We have explored these points in other papers on the debate. For instance, Tan (2005) employs regression tree methods similar to those used in Durlauf and Johnson (1996) to uncover multiple regimes that classify countries into different convergence clubs. A related but conceptually different approach to modeling parameter heterogeneity and nonlinearities has been taken by Durlauf, Kourtellos, and Minkin (2001) and Mamuneas, Savvides, and Stengos, (2006). These papers have employed varying coefficient models that allow the parameters of the model to vary smoothly as opposed to abruptly in the case of sample splitting methods with a threshold variable. However, these previous studies have assumed that the threshold variable is exogenous. This assumption may be plausible if geography variables or, perhaps, ethnic fractionalization variables were responsible for the threshold effect, but not if institutional quality was the threshold variable since the literature has argued strongly that institutions are endogenous.

In terms of our findings, our results suggest that Sachs’ conclusion is only valid for countries with quality of institutions above a threshold level. For low-quality institutions countries, the one factor that appears to have a significant positive impact on economic performance is the degree of trade openness. These results differ from the ones obtained from methods that either ignore the presence of thresholds altogether or ignore the possible endogeneity of the threshold variable.

The paper is organized as follows. Section 2 describes the model and the setup. Section 3

describes the estimator and the main arguments. Section 4 presents our extensive Monte Carlo experiments. Section 5 illustrates our estimator via the empirical example discussed above and section 6 concludes.

2 The Threshold Regression with Endogenous Thresholds (THRET) model

We assume that $\{y_i, x_i, q_i, u_i\}_{i=1}^n$ is strictly stationary, ergodic and ρ -mixing and that $E(u_i|\mathcal{F}_{i-1})=0$ where y_i is the dependent variable, x_i is a $p \times 1$ vector of covariates and q_i is a threshold variable. Let us first consider the simple case of endogeneity in the threshold alone so that x_i is exogenous and does not include q_i . In this case the $l \times 1$ vector of instruments is given by $z_i = (z_{1i}, z_{2i})$, where $z_{2i} = x_i$.

Consider the following THRET model,

$$y_i = x_i' \beta_1 + u_{1i}, \quad q_i \leq \gamma \tag{2.1}$$

$$y_i = x_i' \beta_2 + u_{2i}, \quad q_i > \gamma \tag{2.2}$$

$$q_i = z_i' \pi + v_i \tag{2.3}$$

Equations (2.1) and (2.2) describe the relationship between the variables of interest in each of the two regimes, q_i is the threshold variable with γ being the sample split (threshold) value. Equation (2.3) is the selection equation that determines the regime that applies. Note that q_i is observed but the sample split value is unknown.

The variance covariance matrix of the errors $(u_{1i}, u_{2i}, v)'$ has the following properties. $E(u_{1i}, u_{2i}) = 0$, $E(u_{1i}v_i) = \sigma_{u_1v} \neq 0$, $E(u_{2i}v_i) = \sigma_{u_2v} \neq 0$, $E(u_{1i}^2) = \sigma_1^2 > 0$, $E(u_{2i}^2) = \sigma_2^2 > 0$, and $E(v_i^2) = \sigma_v^2 = 1$ due to a normalization. Notice that if $\sigma_{u_1v} = \sigma_{u_2v} = 0$ then we get the exogenous threshold model as in Seo and Linton (2005) that allow the threshold variable to be a linear index of observed variables. If, further, q_i is exogenously given then we get the threshold regression model of Hansen (2000) and Caner and Hansen (2004). Estimation in these two latter models is based on TR-CLS and IVTR-C2SLS, respectively.

One may be tempted to use a naive (plug-in) estimator as in the case of endogeneity in the slope and

use a naive concentrated two stage least squares method by replacing q_i with the fitted values from a first stage regression, \hat{q}_i and then minimize the concentrated least squares criterion. However, such a strategy will not work and the resulting estimator will not be consistent $\hat{\gamma}_{NAIVE-CLS}^* - \gamma = O_p(1)$ because the conditional mean zero property of the errors is not restored due to omitted bias correction terms.

To see this let us define the indicator variable

$$I_i = \begin{cases} 1 & \text{iff } v_i \leq \gamma - z_i' \pi : \text{Regime 1} \\ 0 & \text{iff } v_i > \gamma - z_i' \pi : \text{Regime 2} \end{cases} \quad (2.4)$$

Let us also assume that that joint distribution between u_{1i} and v_i is given as

$$\begin{pmatrix} u_{1i} \\ v_i \end{pmatrix} | x_i, z_i \sim N \left(0, \begin{pmatrix} \sigma_{u_1}^2 & \sigma_{u_1 v} \\ \sigma_{u_1 v} & 1 \end{pmatrix} \right) \quad (2.5)$$

and using the following standard transformation

$$\begin{pmatrix} \varepsilon_{1i} \\ v_i \end{pmatrix} = \begin{pmatrix} 1 & -\sigma_{u_1 v} \\ 0 & 1 \end{pmatrix} \begin{pmatrix} u_{1i} \\ v_i \end{pmatrix} \quad (2.6)$$

we can get that

$$\begin{pmatrix} \varepsilon_{1i} \\ v_i \end{pmatrix} | x_i, z_i \sim N \left(0, \begin{pmatrix} \sigma_1^2 - \sigma_{u_1 v}^2 & 0 \\ 0 & 1 \end{pmatrix} \right) \quad (2.7)$$

Similarly we can define the joint distribution between u_{2i} and v_i and also introduce ε_{2i} in the same way as we did ε_{1i} to be uncorrelated with v_i . Let $\kappa_1 = \sigma_{u_1 v} = \rho_1 \sigma_{u_1}$, $\kappa_2 = \sigma_{u_2 v} = \rho_2 \sigma_{u_2}$, and define

$$u_{1i} = \kappa_1 v_i + \varepsilon_{1i} = \kappa_1 \lambda_1 (\gamma - z_i \pi) + e_{1i} \quad (2.8)$$

$$u_{2i} = \kappa_2 v_i + \varepsilon_{2i} = \kappa_2 \lambda_2 (\gamma - z_i \pi) + e_{2i} \quad (2.9)$$

we have the following conditional expectations for each of the regimes

$$E(y | x_1, z_1, v_i \leq \gamma - z_i' \pi) = x_i \beta_1 + \kappa_1 \lambda_{1i} (\gamma - z_i' \pi) \quad (2.10)$$

$$E(y|x_2, z_2, v_i > \gamma - z'_i\pi) = x_i\beta_2 + \kappa_1\lambda_{2i}(\gamma - z'_i\pi) \quad (2.11)$$

where $\lambda_1(\gamma - z'_i\theta) = -\frac{\phi(\gamma - z'_i\theta)}{\Phi(\gamma - z'_i\theta)}$ and $\lambda_2(\gamma - z'_i\theta) = \frac{\phi(\gamma - z'_i\theta)}{1 - \Phi(\gamma - z'_i\theta)}$ are the inverse Mills bias correction terms.

We can also rewrite the THRET model (2.1), (2.2), and (2.3) as a single equation. Let $\lambda_i = \lambda_i(\gamma - z'_i\pi) = d(\gamma)\lambda_{1i} + (1 - d(\gamma))\lambda_{2i}$, $\tilde{\lambda}_{1i} = d(\gamma)\lambda_{1i}$, $e_i = d(\gamma)e_{1i} + (1 - d(\gamma))e_{2i}$, $\delta_\kappa = (\kappa_1 - \kappa_2)$, $\beta = \beta_2$, and $\kappa = \kappa_2$ then we get

$$y_i = x'_i\beta + x_i(\gamma)'\delta_\beta + \kappa\lambda_i(\gamma - z'_i\pi) + \delta_\kappa\tilde{\lambda}_{1i}(\gamma - z'_i\pi) + e_i \quad (2.12)$$

where $d_i(\gamma) = I(q_i \leq \gamma)$ and $x_i(\gamma) = x_id_i(\gamma)$.

It is easy to see that in the case when the two regimes enjoy the same error structure $u_1 = u_2$, or when there is no regime dependent heteroskedasticity, we simply get

$$y_i = x_i\beta + x_i(\gamma)'\delta_\beta + \kappa\lambda_i(\gamma - z'_i\pi) + e_i \quad (2.13)$$

and when $\rho = 0$ and hence $\kappa = 0$ we get Hansen's (2000) Threshold Regression for exogenous threshold and slope variables model,

$$y_i = x_i\beta + x_i(\gamma)'\delta_\beta + e_i \quad (2.14)$$

It is also apparent that THRET is similar in nature to the case of the error interdependence that exists in limited dependent variable models between the equation of interest and the sample selection equation, see Heckman (1979). However, there is one important difference. While in sample selection models, we observe the assignment of observations into regimes but the variable that drives this assignment is taken to be latent, here, it is the opposite; we do not know which observations belong to which regime (we do not know the threshold value), but we can observe the threshold variable.

2.1 Estimation

Our estimation procedure proceeds in three steps. First, we estimate the parameter vector π in the threshold equation (2.3) by Least Squares (LS). Second, we estimate the threshold estimate by minimizing a concentrated two stage least squares (THRET-C2SLS) criterion using the estimates of $\hat{\pi}$ from the first stage

$$S_n^{C2SLS}(\beta(\gamma), \delta_\beta(\gamma), \delta_\kappa(\gamma), \kappa(\gamma), \gamma) = \sum_{i=1}^n (y_i - x_i'\beta - x_i'(\gamma)\delta_\beta - \kappa\lambda_i(\gamma - z_i'\hat{\pi}) - \delta_\kappa\tilde{\lambda}_{1i}(\gamma - z_i'\hat{\pi}))^2 \quad (2.15)$$

Third, we estimate the LS estimates of the slope parameters based on the split samples implied by $\hat{\gamma}_{THRET-C2SLS}$.

This sum of squared errors criterion (2.15) implies that Hansen's TR-CLS criterion which is used for estimation of (2.14) will yield an inconsistent estimator for the THRET model given by equations (2.1), (2.2), and (2.3), where

$$S_n^{CLS}(\beta(\gamma), \delta_\beta(\gamma), \delta_\kappa(\gamma), \gamma) = \sum_{i=1}^n (y_i - x_i'\beta - x_i'(\gamma)\delta_\beta)^2 \quad (2.16)$$

since it can be shown that $S_n^{C2SLS}(\beta, \delta_\beta, \delta_\kappa, \kappa, \gamma) = S_n^{CLS}(\beta, \delta, \gamma) + O_p(1)$.

Proposition 1: Consistency of C2SLS Estimator in THRET For the C2SLS estimator in the case of endogenous threshold but exogenous slope variables defined as $\hat{\gamma}_{C2SLS} = \arg \min (S_n^{C2SLS}(\gamma) - e'e)$ we have that $\hat{\gamma}_{THRET-C2SLS} \xrightarrow{P} \gamma_0$.

In the appendix we provide a proof that uses similar regularity conditions as Hansen (2000).

3 The Threshold Regression with Endogenous Threshold and Slope model (THRETS)

In this section we generalize THRET to the more realistic case of a Threshold Regression with Endogenous Threshold and Slope (THRETS) variables. THRETS takes the form of

$$y_i = x_i'\beta + x_i(\gamma)'\delta_\beta + \kappa\lambda_i(\gamma - z_i'\pi) + \delta_\kappa\tilde{\lambda}_{1i}(\gamma - z_i'\pi) + e_i \quad (3.17)$$

and

$$x_i = \Pi'z_i + \eta_i \quad (3.18)$$

where the $l \times 1$ vector $z_i = (z_{1i}, z_{2i})$ with $z_{2i} = x_{2i}$ and $E(\eta_i|z_i) = 0$, and where $l \geq p$. π_1 is the parameter vector of the regression of q_i on z_i such that $\Pi = (\pi_1, \Pi_2)$.

Again we propose an estimation procedure based on three steps. First, we estimate the parameter vector Π in the threshold equation (3.18) by LS. Second, we estimate the sample split (threshold) value by minimizing a Concentrated Two Stage Least Squares (C2SLS) criterion using the estimates of $\hat{\Pi}$ from the first stage

$$S_n^{C2SLS}(\beta(\gamma), \delta_\beta(\gamma), \delta_\kappa(\gamma), \kappa(\gamma), \gamma) = \sum_{i=1}^n (y_i - \hat{x}_i' \beta - \hat{x}_i'(\gamma) \delta_\beta - \kappa \lambda_i(\gamma - z_i' \hat{\pi}_1) - \delta_\kappa \tilde{\lambda}_{1i}(\gamma - z_i' \hat{\pi}_1))^2 \quad (3.19)$$

Third, we estimate the slope parameters using 2SLS or GMM on the split samples implied by the estimate of γ .

Using a similar framework as in Caner and Hansen (2004) it can be shown that $\hat{\gamma}_{THRETS-C2SLS} = \arg \min (S_n^{C2SLS}(\gamma) - e'e)$ is consistent.

4 Monte Carlo

We proceed below with an exhaustive simulation study that compares the small sample performance of our estimator against existing estimators. In particular, when we allow for the endogeneity of the threshold alone we compare THRET-C2SLS estimates of the threshold parameter against estimates based on TR-CLS (Hansen, 2000) and a naive C2SLS estimator (NAIVE-C2SLS) that simply uses the fitted values from a first stage as a threshold variable. We also compare the LS estimates of the slope coefficients that are based on the subsamples implied by $\hat{\gamma}$. Likewise when we allow for the endogeneity of both the slope and the threshold variable we compare our estimator against the IVTR-C2SLS (Hansen, 2004), and the naive C2SLS estimator (NAIVE-C2SLS) that replaces both the threshold and the slope variables with the fitted values from a first stage and then minimizes a concentrated least squares criterion. In this case we compare the GMM estimates of the slope coefficients for the various estimators.

The Monte Carlo design is based on the following threshold regression

$$y_i = \begin{cases} x_i' \beta_1 + u_i, & q_i \leq 2 \\ x_i' \beta_2 + u_i, & q_i > 2 \end{cases} \quad (4.20)$$

The threshold equation is given by

$$q_i = 2 + 3z_{1i} + 3z_{2i} + v_i \quad (4.21)$$

where $v_i, \varepsilon_i \sim NIID(0, 1)$ and $u_i = \sigma_u^2(\rho_0 v_i + (1 - \rho_0)\varepsilon_i) / \sqrt{(\rho_0^2 + (1 - \rho_0)^2)}$ so that the degree of the endogeneity is controlled via the correlation between u_i and v_i given by $\rho = \rho_0 / \sqrt{(\rho_0^2 + (1 - \rho_0)^2)}$. We specify $\rho_0 = 0.05, 0.50, \text{ and } 0.95$. We fix $\beta_2 = 1$ and vary β_1 by examining various $\delta = \beta_1 - \beta_2$, $\delta = (0.01, 0.05, 0.1, 0.25, 0.5, 1)$. First, we examine the case where the threshold variable is the only endogenous variable $x_i = (1, x_{2i})$ and second, we look into the more realistic case that allows for both endogeneity in the threshold and the slope variables $x_i = (1, q_i, x_{2i})$. Furthermore, we consider the implications of the degree of correlation between the (excluded) instrumental variables z_i and the exogenous slope variables x_{2i} through $z_{ij} = (\omega_0 x_{2i} + (1 - \omega_0)\xi_{ij}) / \sqrt{(\omega_0^2 + (1 - \omega_0)^2)}$, where $\xi_{ij} \sim NIID(0, 1)$ and $\omega_0 / \sqrt{(\omega_0^2 + (1 - \omega_0)^2)}$ is the degree of correlation between z_i and x_{2i} . Finally, we consider sample sizes of 100, 200, and 500 using 1000 Monte Carlo simulations.

Tables 1-3 discuss the relative Mean Square Error (MSE) while Figures 1-7 present the Gaussian kernel density estimates using Silverman's bandwidth parameter of the Monte Carlo estimates of the threshold coefficient γ and the difference of slope coefficients $\delta = \beta_1 - \beta_2$ of the various estimators.

First we consider the estimation of the threshold γ in 2.1, 2.2, and 2.3 in the case of endogeneity in the threshold alone. Table 1(a) presents the relative MSEs of TR-CLS and NAIVE-C2SLS relative to THRET-C2SLS estimator given by MSE_{TR}/MSE_{THRET} and MSE_{NAIVE}/MSE_{THRET} , respectively, across different values of δ , different quantiles and sample sizes n when $\rho_0 = 0.95$ and $\omega_0 = 0.95$. For all δ and all sample sizes the relative MSEs show that THRET is relatively more efficient than CLS and NAIVE-2SCLS. These efficiencies are largest for the right tail as shown by the 95th quantile of standard error. Similarly, Table 1(b) demonstrates the relative efficiency of THRET-C2SLS when there is endogeneity in both the threshold and slope variables using MSE_{IVTR}/MSE_{THRETS} and MSE_{NAIVE}/MSE_{THRETS} across different values of δ , different quantiles and sample sizes n when $\rho_0 = 0.95$ and $\omega_0 = 0.95$. Figures 1-2 show the corresponding kernel density estimates of the threshold estimator for various values of δ . Figures 6-7 show for $\delta = 0.5$ the kernel density estimates of the threshold estimator for various degrees of endogeneity $\rho_0 = 0.05, 0.50, 0.95$.¹ It is evident that the distribution of THRET-C2SLS and THRETS-C2SLS centers around the true value and dominates its competitors in terms of efficiency. Under the assumption of small thresholds effects in the sense that $\delta_{\beta, n} \rightarrow 0$ as $n \rightarrow \infty$, the asymptotic distribution of the threshold estimator is a suitably modified version of the non-standard distribution derived by Hansen (2000) and by Caner and Hansen (2000) for the case of exogenous

¹We have conducted experiments across different degrees of threshold endogeneity (different values of ρ) and a broad range of values of δ . Although these experiments are not reported in detail to conserve space, they are available from the authors on request.

and endogenous regressors, respectively. This is verified by the figures that we obtained for the different values of δ .

In terms of slope coefficients our estimator performs at least as well as the respective competitors. Tables 2(a) presents the relative MSEs of the LS estimates and Table 2(b) presents the relative MSEs of the GMM estimates of the slope coefficient of the exogenous covariate of THRET and THRETS, respectively. Similarly, Table 3 presents the relative MSEs of the GMM estimates of the slope coefficient of the endogenous covariate. Figures 3-5 present the corresponding kernel density estimates.

In the interests of robustness, we also investigated what happened when we varied the degree of the correlation between the instrumental variables z and the exogenous slope variables x_2 . As in the case of Heckman's estimator, THRET-C2SLS and THRETS-C2SLS become more efficient as ω decreases and the degree of multicollinearity between $\pi'z$ and x is small. Furthermore, our findings are also robust to regime dependent heteroskedasticity. Due to space limitations these experiments are not reported in detail but they are all available from the authors on request.

5 Empirical Example

In this section, we revisit the institutions versus geography debate using our THRET methods, as discussed in the Introduction. The data we use comes primarily from Easterly and Levine (2003). As mentioned above, the dependent variable is the log of GDP per capita in 1995. We include a variable that measures trade openness and a variable that measures ethnic diversity. We also include a proxy for institutional quality, the average (over 1985-95) expropriation risk variable, from the International Country Risk Guide (ICRG). Finally, we augment the Easterly-Levine dataset with Sachs' preferred malaria variable (MALFAL94p) from the Harvard Center for International Development (CID). Following Acemoglu, Johnson, and Robinson (2001) we instrument institutional quality (which is assumed to be endogenous) using the log of European settler mortality.

We contrast results where the model is assumed to be linear against those where the model is a THRETS model with institutional quality as the (endogenous) threshold variable. Table 4 presents the results. Our objective in these exercises is not to embark on a thorough re-examination of this important debate, but rather to highlight how taking Sachs' methodological critique above (see, Introduction) seriously can lead to new and important insights. In all cases, we find that our THRETS-C2SLS results deliver more nuance interpretations of established findings.

For example, column 1 of Table 4 shows the linear 2SLS results for a regression of per capita GDP on institutional quality and malaria. These results for the linear model appear to support Sachs'

finding that “malaria transmission, which is strongly affected by ecological conditions, directly affects the level of per capita income after controlling for the quality of institutions [Sachs (2003), Abstract]”. However, our THRETS-C2SLS results (see, column 2 of Table 4) suggest that this finding for malaria is only true when the quality of institutions is above a threshold level. Below that threshold level, neither institutions nor disease ecology appears to have any effect on a country’s economic performance. This result is maintained even if we include Easterly and Levine’s ethnic diversity variable as another growth determinant (see column 4 of Table 4). In columns 5 and 6 of Table 4 where we also include the trade openness variable as a growth determinant, we find that Rodrik, Subramanian, and Trebbi (2004) may have under-sold the importance of macroeconomic policies that promote a more open economy when they claim that “once institutions are controlled for, trade is almost always insignificant [Rodrik, et al, Abstract]”. Their claims certainly appear to be true when we assume a linear model (see, column 5 of Table 4). However, our THRETS-C2SLS results suggest that for low-quality institutions countries, trade openness may be one of the only factors that has a significant positive impact on economic performance. For high-quality institutions countries, on the other hand, good institutions promote economic performance while higher levels of ethnic diversity detract from it.²

We also carried out a series of robustness checks (unreported) where we included other macroeconomic policy variables that are commonly employed in the literature, such as inflation and real exchange rate overvaluation, as additional growth determinants. We also included other fundamental determinants such as religious affiliation shares for Catholics, Muslims, and Other Religions on the righthand-side. We carried out exercises that included various combinations of these regressors along with those described above. In most cases, we found that the results for the THRETS-C2SLS model differed substantially from those for the linear model. Overall, we conclude that there is much evidence to suggest that there exists substantial heterogeneity in the growth experiences of countries, and that studies that seek to promote mono-causal explanations for the variation in long-run economic performance across countries are potentially misleading.

6 Conclusion

In this paper we propose an extension of Hansen (2000) and Caner and Hansen (2004) that deals with the endogeneity of the threshold variable. We developed a concentrated two stage least squares

²As in Hansen (2000) we compute a heteroskedasticity corrected asymptotic confidence interval for threshold estimate using a quadratic polynomial. One difference is that the nuisance parameters in the conditional variance is estimated via a polynomial regression in \hat{q} and \hat{q}^2 instead of q and q^2 . \hat{q} and \hat{q}^2 are the fitted values from LS regressions of q and q^2 on the set of instruments z . Simulated coverage probabilities of a nominal coverage of 90% interval provides support to our proposal. Due to space limitations these experiments are not reported but they are all available from the authors on request.

estimator that deals with the problem of endogeneity in the threshold variable by generating a correction term based on the inverse Mills ratios to produce consistent estimates for the threshold parameter and the slope coefficients. By means of an extensive simulation study we examine the performance of our estimator when compared with its competitors. Our proposed estimator performs well for a variety of sample sizes and parameter combinations. We illustrate the usefulness of the proposed estimator by means of an empirical example from economic growth.

References

- [1] Acemoglu, D. Johnson, S. and J. A. Robinson (2001), "The Colonial Origins of Comparative Development: An Empirical Investigation," *American Economic Review*, 91, p. 1369-1401.
- [2] Caner, M. and B. Hansen. (2004), "Instrumental Variable Estimation of a Threshold Model," *Econometric Theory*, 20, p. 813-843.
- [3] Chan, K. S. (1993), "Consistency and Limiting Distribution of the Least Squares Estimator of a Threshold Autoregressive Model," *The Annals of Statistics*, 21, p. 520-533.
- [4] Dhrymes, P. J. (2004), "Limited Information Estimation of Simultaneous Equations with Indicator Endogenous Variables", Columbia University, mimeo.
- [5] Durlauf, S., A. Kourtellos, and A. Minkin, (2001), "The Local Solow Growth Model," *European Economic Review*, 45, 4-6, p. 928-40.
- [6] Durlauf, S. N., and P. A. Johnson (1995), "Multiple Regimes and Cross Country Behavior", *Journal of Applied Econometrics*, 10(4), p. 365-384.
- [7] Easterly, W. and R. Levine (2003), "Tropics, Germs, and Crops: How Endowments Influence Economic Development," *Journal of Monetary Economics*, 50(1), p. 3-39.
- [8] Gonzalo, J. and M. Wolf (2005), "Subsampling Inference in Threshold Autoregressive Models," *Journal of Econometrics*, 127(2), p. 201-224.
- [9] Hansen, B. E. (2000), "Sample Splitting and Threshold Estimation," *Econometrica*, 68(3), p. 575-604.
- [10] Heckman, J. (1979), "Sample Selection Bias as a Specification Error," *Econometrica*, 47(1), p. 153-161.
- [11] Mamuneas, T., A. Savvides, and T. Stengos, (2006), "Economic Development and Return to Human Capital: A Smooth Coefficient Semiparametric Approach," *Journal of Applied Econometrics*, 21(1), p. 111-132.
- [12] Rodrik, D., A. Subramanian, and F. Trebbi (2004), "Institutions Rule: The Primacy of Institutions over Geography and Integration in Economic Development," *Journal of Economic Growth*, 9(2), p.131-165.
- [13] Sachs, J. (2003), "Institutions Don't Rule: Direct Effects of Geography on Per Capita Income," National Bureau of Economic Research Working Paper No. 9490.

- [14] Seo, M. H. and O. Linton (2007), “A Smoothed Least Squares Estimator For Threshold Regression Models,” *Journal of Econometrics*, 141(2), p. 704-735.
- [15] Tan, C. M. (2005), “No One True Path: Uncovering the Interplay between Geography, Institutions, and Fractionalization in Economic Development”, Tufts University, Working Paper No. 2005-12.

Appendix

A Consistency of $\widehat{\gamma}_{C2SLS}$. Proof of Proposition 1

Let us define the $n \times 1$ vector Y , the $n \times p$ matrix X and the $n \times l$ matrix Z by stacking y_i , x_i and z_i , respectively. We also define X_γ to be the $n \times l$ matrix with typical i -th row $x_i(\gamma) = x_i d_i(\gamma)$, where as before $d(\gamma) = I(q_i \leq \gamma)$ and similarly Λ_γ to be the matrix with typical element $d(\gamma)\lambda_{1i}$. Let us also define the $n \times 1$ vector $\Lambda(\gamma) = d(\gamma)\lambda_1(\gamma) + (1 - d(\gamma))\lambda_2(\gamma)$.

At γ_0 , $\Lambda(\gamma_0) = \Lambda(0)$, $X_{\gamma_0} = X_0$, $\Lambda_{\gamma_0} = \Lambda_0$. In the spirit of Hansen (2000), we define $\widetilde{X}_\gamma = (X_\gamma, \Lambda_\gamma)$, $\widetilde{X}(\gamma) = (X, \Lambda(\gamma))$, $\widetilde{X}_\gamma^* = (\widetilde{X}_\gamma, \widetilde{X}(\gamma) - \widetilde{X}_\gamma)$ and using similar regularity conditions we assume that

$$\begin{aligned} \frac{1}{n} \widetilde{X}'_\gamma \widetilde{X}_\gamma &\xrightarrow{p} M(\gamma) \\ \frac{1}{n} \widetilde{X}'_{\gamma_0} \widetilde{X}_{\gamma_0} &\xrightarrow{p} M(\gamma_0) \\ \frac{1}{n} \widetilde{X}'_{\gamma_0} \widetilde{X}_\gamma &\xrightarrow{p} M(\gamma_0) \\ \frac{1}{n} (\widetilde{X}(\gamma_0) - \widetilde{X}_{\gamma_0})' \widetilde{X}_\gamma &\xrightarrow{p} 0 \end{aligned}$$

The last condition guarantees that asymptotically the matrix of cross products between $\widetilde{X}_{\gamma_0}^*$ and \widetilde{X}_γ^* for $\gamma \geq \gamma_0$ is diagonal.

We also have that

$$\begin{aligned} p \lim_{n \rightarrow \infty} \frac{1}{n} \begin{pmatrix} \widetilde{X}'_0 \widetilde{X}_0 & 0 \\ (\widetilde{X}(0) - \widetilde{X}_0)' \widetilde{X}_\gamma & (\widetilde{X}(\gamma) - \widetilde{X}_\gamma)' (\widetilde{X}(\gamma) - \widetilde{X}_\gamma) \end{pmatrix} = \\ \begin{pmatrix} M(\gamma_0) & 0 \\ 0 & p \lim_{n \rightarrow \infty} \frac{1}{n} (\widetilde{X}(\gamma) - \widetilde{X}_\gamma)' (\widetilde{X}(\gamma) - \widetilde{X}_\gamma) \end{pmatrix} = M(\gamma_0, \gamma) \end{aligned}$$

We then define the projection matrix spanned by the columns of \widetilde{X}_γ^* .

$$\widetilde{P}_\gamma^* = \widetilde{X}_\gamma^* \left(\widetilde{X}_\gamma^{*'} \widetilde{X}_\gamma^* \right)^{-1} \widetilde{X}_\gamma^{*'} \quad (\text{A.1})$$

Let us rewrite the model as

$$Y = X\theta + X_0\delta + \rho\Lambda(0) + \phi\Lambda_0 + \varepsilon \quad (\text{A.2})$$

or

$$Y = \tilde{X}(0)\alpha + \tilde{X}_0\psi + \varepsilon \quad (\text{A.3})$$

So we have

$$S_n(\gamma) - \varepsilon'\varepsilon = Y' \left(I - \tilde{P}_\gamma^* \right) Y - \varepsilon'\varepsilon \quad (\text{A.4})$$

Then as in Hansen (2000) for $\psi_n = Cn^{-\mu}$ with $C \neq 0$ and $0 < \mu < \frac{1}{2}$

$$\begin{aligned} & n^{-1+2\mu} (S_n(\gamma) - \varepsilon'\varepsilon) \\ &= n^{-1+2\mu} \left[\left(\tilde{X}(0)\alpha_n + \tilde{X}_0\psi_n + \varepsilon \right)' \left(I - \tilde{P}_\gamma^* \right) \left(\tilde{X}(0)\alpha_n + \tilde{X}_0\psi_n + \varepsilon \right) - \varepsilon'\varepsilon \right] \\ &= n^{-1} \left[C'_1 \tilde{X}'(0) \left(I - \tilde{P}_\gamma^* \right) \tilde{X}(0) C_1 + C'_2 \tilde{X}'(0) \left(I - \tilde{P}_\gamma^* \right) \tilde{X}_0 C_2 + C'_3 \tilde{X}'_0 \left(I - \tilde{P}_\gamma^* \right) \tilde{X}_0 C_3 \right] + o_p(1) \\ &= C'_1 \left(\frac{\tilde{X}'(0)\tilde{X}(0)}{n} \right) C_1 - C'_1 \left(\frac{\tilde{X}'(0)\tilde{X}_\gamma^*}{n} \right) \left(\frac{\tilde{X}_\gamma^* \tilde{X}_\gamma^*}{n} \right)^{-1} \left(\frac{\tilde{X}_\gamma^* \tilde{X}(0)}{n} \right) C_1 + \\ & \quad C'_2 \left(\frac{\tilde{X}'(0)\tilde{X}_0}{n} \right) C_2 - C'_2 \left(\frac{\tilde{X}'(0)\tilde{X}_\gamma^*}{n} \right) \left(\frac{\tilde{X}_\gamma^* \tilde{X}_\gamma^*}{n} \right)^{-1} \left(\frac{\tilde{X}_\gamma^* \tilde{X}_0}{n} \right) C_2 + \\ & \quad C'_3 \left(\frac{\tilde{X}'_0 \tilde{X}_0}{n} \right) C_3 - C'_3 \left(\frac{\tilde{X}'_0 \tilde{X}_\gamma^*}{n} \right) \left(\frac{\tilde{X}_\gamma^* \tilde{X}_\gamma^*}{n} \right)^{-1} \left(\frac{\tilde{X}_\gamma^* \tilde{X}_0}{n} \right) C_3 + o_p(1) \\ &= C' \left[\left(\frac{\tilde{X}'_0 \tilde{X}_0}{n} \right) - \left(\frac{\tilde{X}'_0 \tilde{X}_\gamma^*}{n} \right) \left(\frac{\tilde{X}_\gamma^* \tilde{X}_\gamma^*}{n} \right)^{-1} \left(\frac{\tilde{X}_\gamma^* \tilde{X}_0}{n} \right) \right] C + o_p(1) \end{aligned}$$

That is,

$$\begin{aligned} & n^{-1+2\mu} (S_n(\gamma) - \varepsilon'\varepsilon) \\ &= C' \left[\left(\frac{\tilde{X}'_0 \tilde{X}_0}{n} \right) - \left(\frac{\tilde{X}'_0 \tilde{X}_\gamma^*}{n} \right) \left(\frac{\tilde{X}_\gamma^* \tilde{X}_\gamma^*}{n} \right)^{-1} \left(\frac{\tilde{X}_\gamma^* \tilde{X}_0}{n} \right) \right] C + o_p(1) \end{aligned} \quad (\text{A.5})$$

It can be shown that

$$n^{-1+2\mu} (S_n(\gamma) - \varepsilon'\varepsilon) \xrightarrow{p} C' \left[M(\gamma_0) - M(\gamma_0, \gamma) M(\gamma)^{-1} M(\gamma_0, \gamma)' \right] C \quad (\text{A.6})$$

Let

$$b_1(\gamma) = C' \left[M(\gamma_0) - M(\gamma_0, \gamma) M(\gamma)^{-1} M(\gamma_0, \gamma)' \right] C$$

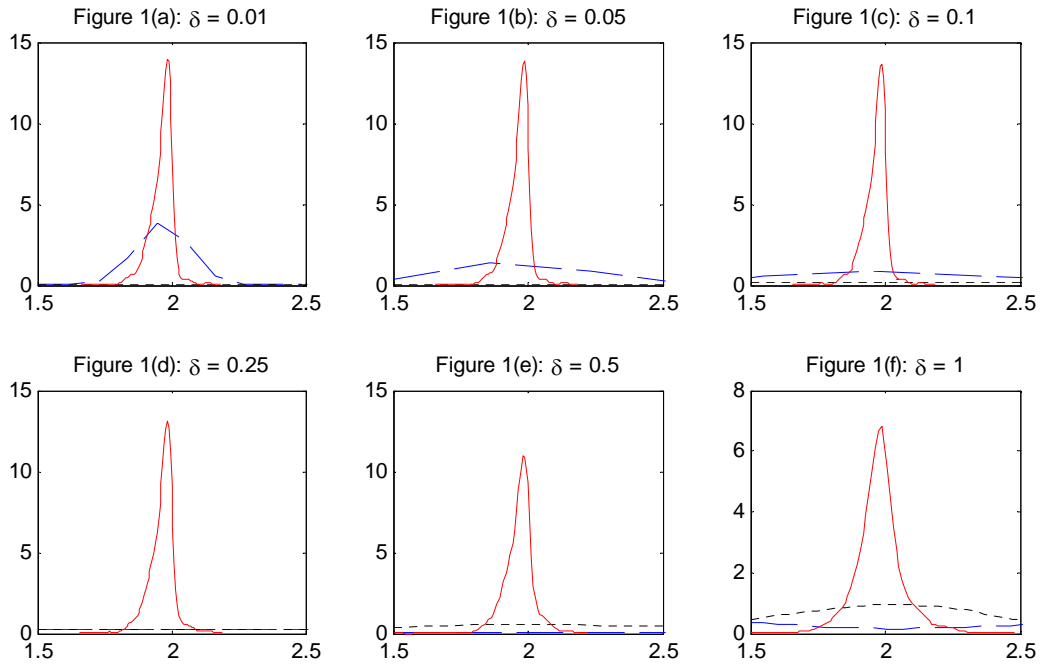
Following similar arguments as in Hansen (2000, Lemma A.5) it can be shown that $\frac{d}{d\gamma} b_1(\gamma_0) > 0$ and $b_1(\gamma)$ is continuous and weakly increasing so that $b_1(\gamma)$ is uniquely minimized at γ_0 over $[\gamma_0, \bar{\gamma}]$. A similar argument can be made for $\gamma \in [\underline{\gamma}, \gamma_0]$, so that $b_2(\gamma)$ which is suitably defined is uniquely minimized at γ_0 .

So uniformly over all values of γ ,

$$n^{-1+2\mu} (S_n^*(\gamma) - \varepsilon' \varepsilon) \xrightarrow{p} b_1(\gamma) 1_{\{\gamma > \gamma_0\}} + b_2(\gamma) 1_{\{\gamma \leq \gamma_0\}} \quad (\text{A.7})$$

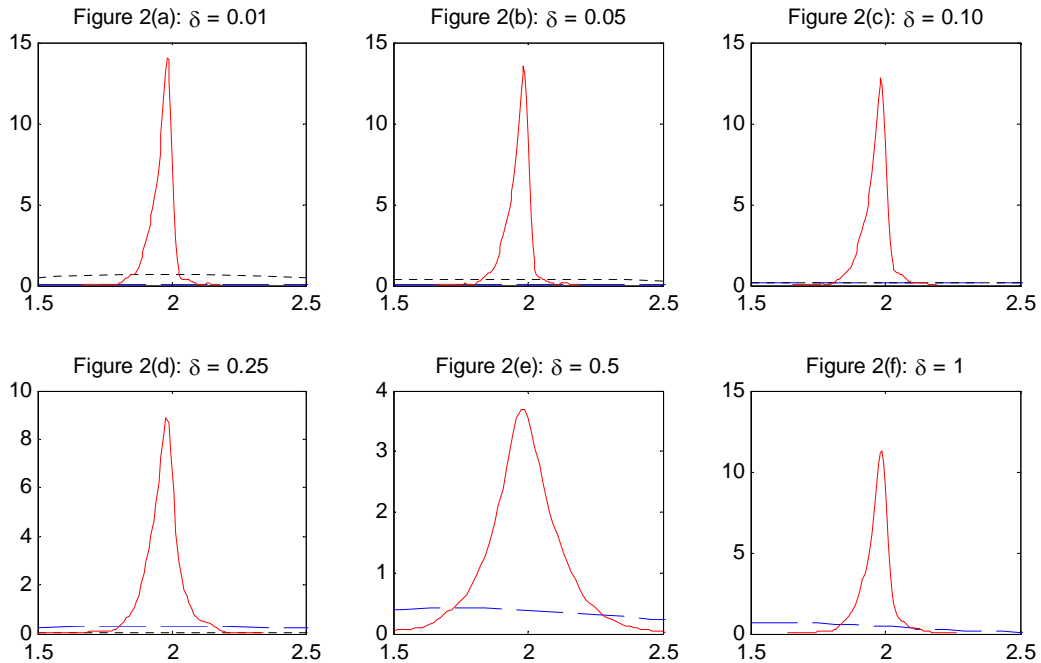
Since $\hat{\gamma}_{C2SLS} = \arg \min (S_n^*(\gamma) - \varepsilon' \varepsilon)$, we get that $\hat{\gamma}_{C2SLS} \xrightarrow{p} \gamma_0$.

Figures 1(a) – (f) : MC Kernel Densities of the Threshold Estimate (endogeneity in the threshold alone)



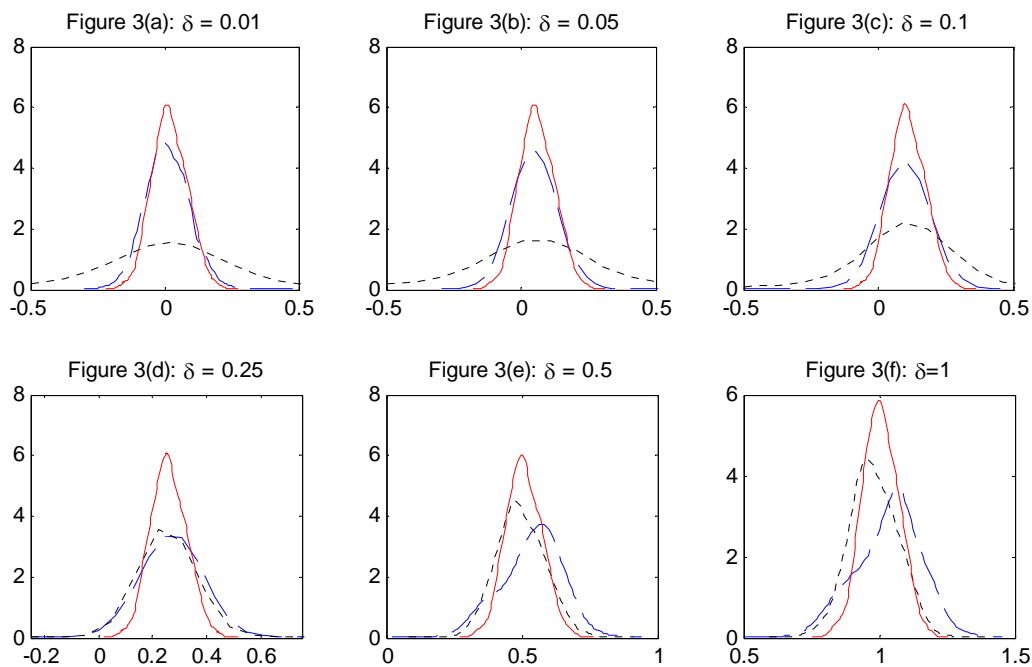
Note: “The solid line represents THRET-C2SLS, the dashed line represents TR-CLS, and the dotted line represents NAIVE-CLS.”

Figures 2(a) – (f) : MC Kernel Densities of the Threshold Estimate (endogeneity in both the threshold and slope)



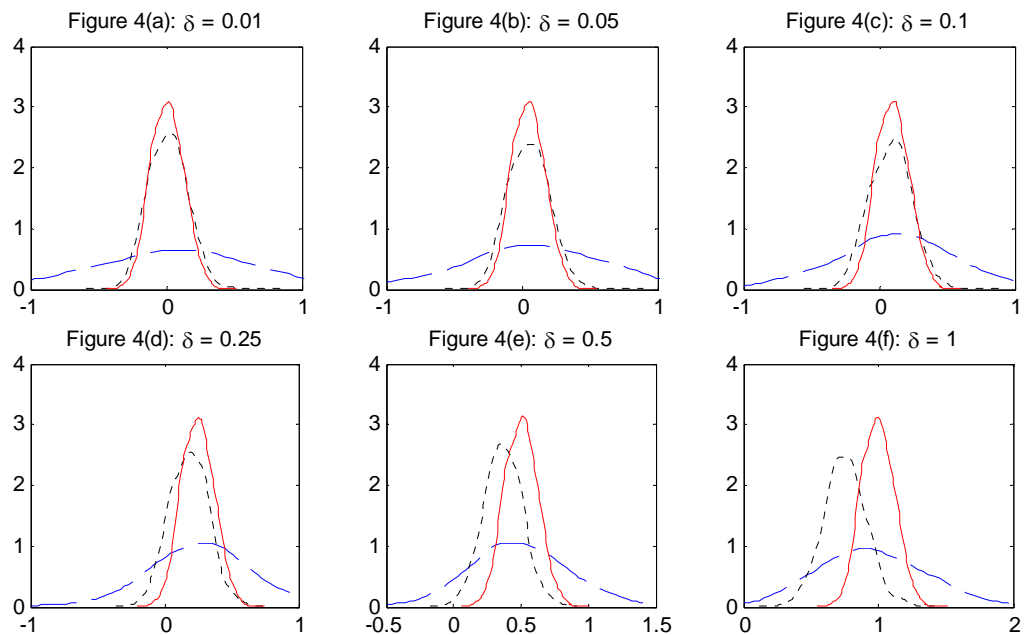
Note: “The solid line represents THRETS-C2SLS, the dashed line represents IVTR-C2LS, and the dotted line represents NAIVE-C2LS.”

Figures 3(a) – (f) : MC Kernel Densities of the Slope Coefficient of the Exogenous Covariate (endogeneity in the threshold alone)



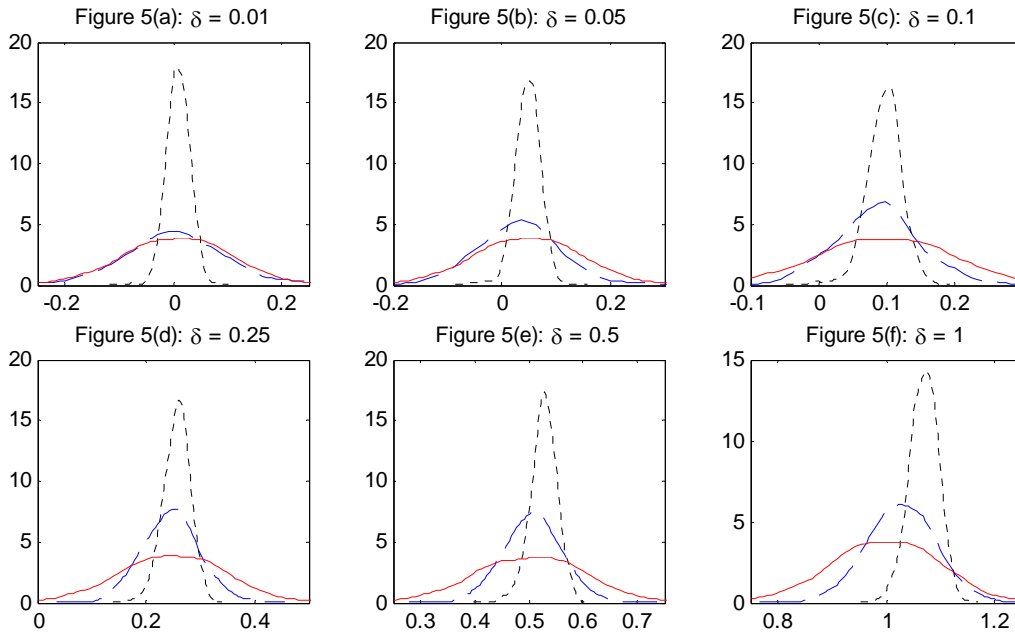
Note: “The solid line represents THRET-LS, the dashed line represents TR-LS, and the dotted line represents NAIVE-LS.”

Figures 4(a) – (f) : MC Kernel Densities of the Slope Coefficient of the Exogenous Covariate (endogeneity in both the threshold and slope)



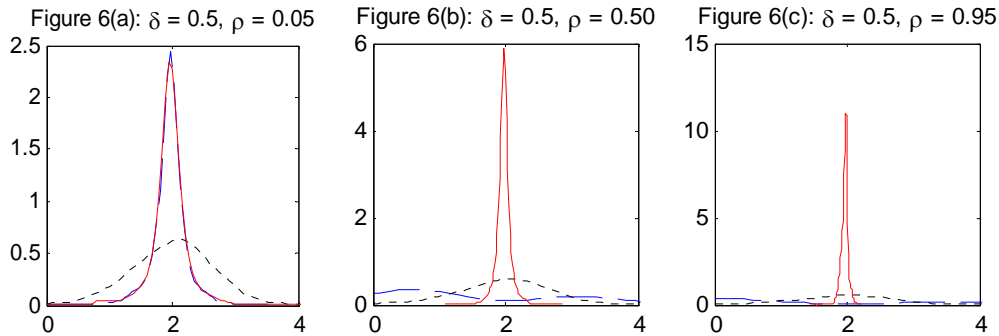
Note: “The solid line represents THRET-GMM, the dashed line represents IVTR-GMM, and the dotted line represents NAIVE-GMM.”

Figures 5(a) – (f) : MC Kernel Densities of the Slope Coefficient of the Endogenous Covariate



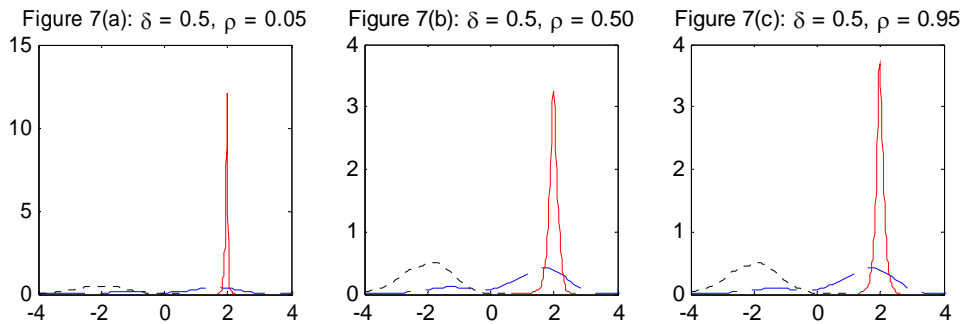
Note: “The solid line represents THRET-GMM, the dashed line represents IVTR-GMM, and the dotted line represents NAIVE-GMM.”

Figures 6(a) – (c) : MC Kernel Densities of the Threshold Estimate for various degrees of endogeneity (endogeneity in the threshold alone)



Note: “The solid line represents THRET-C2SLS, the dashed line represents TR-CLS, and the dotted line represents NAIVE-CLS.”

Figures 7(a) – (c) : MC Kernel Densities of the Threshold Estimate for various degrees of endogeneity (endogeneity in both the threshold and slope)



Note: “The solid line represents THRETS-C2SLS, the dashed line represents IVTR-C2SLS, and the dotted line represents NAIVE-C2SLS.”

Table 1(a): Relative Efficiency of Threshold Estimator $\hat{\gamma}$ (Endogeneity in the threshold alone)

Quantiles	MSE_{TR} / MSE_{THRET}			$MSE_{NAIVE} / MSE_{THRET}$		
	0.05	0.50	0.95	0.05	0.50	0.95
$\delta = 0.01$						
n = 100	2.565	4.134	239.8	506.7	614.7	275.4
n = 200	2.184	2.095	727.7	2474	2471	2189.8
n = 500	1.298	1.372	1.544	7432	28140	23941
$\delta = 0.05$						
n = 100	3.948	6.270	244.2	536.2	649.7	267.1
n = 200	2.940	2.683	1096.3	2946	2285	2139
n = 500	1.193	1.411	1.809	5312	14255	22876
$\delta = 0.10$						
n = 100	4.475	23.33	228.5	512.4	483.5	247.2
n = 200	3.027	4.646	1289	2384	1610	2072
n = 500	1.326	1.630	198.8	1767	4114	19016
$\delta = 0.25$						
n = 100	17.71	230.2	121.1	220.8	137.9	114.5
n = 200	19.35	708.5	1371	742.0	292.3	1191
n = 500	5.367	676.1	2118	726.7	724.0	948.1
$\delta = 0.50$						
n = 100	570.7	109.0	34.63	39.79	22.33	13.64
n = 200	4113	432.3	137.2	118.8	68.49	43.99
n = 500	67296	2964	574.8	152.6	242.9	138.1
$\delta = 1.0$						
n = 100	182.3	21.57	5.248	13.64	5.197	2.585
n = 200	750.7	61.32	16.00	23.86	10.74	5.701
n = 500	4288	398.4	79.38	38.88	40.27	17.07

Table 1(b): Relative Efficiency of Threshold Estimator of $\hat{\gamma}$ (Endogeneity in both the threshold and the slope)

Quantiles	$MSE_{IVTR} / MSE_{THRETS}$			$MSE_{NAIVE} / MSE_{THRETS}$		
	0.05	0.50	0.95	0.05	0.50	0.95
$\delta = 0.01$						
n = 100	15.26	53.15	176.4	547.2	559.3	190.2
n = 200	17.97	34.63	891.1	1607	2905	1325
n = 500	6.346	9.382	1115	11380	23037	10522
$\delta = 0.05$						
n = 100	21.34	175.6	134.1	644.5	499.1	142.5
n = 200	38.18	128.6	947.8	1859	2509	1208
n = 500	9.463	22.74	4553	6246	9967	8900
$\delta = 0.10$						
n = 100	60.27	542.13	55.11	642.9	413.2	52.01
n = 200	159.4	2987	875.9	1256	1169	903.8
n = 500	36.60	14798	5003	2942	3266	4860
$\delta = 0.25$						
n = 100	3259	494.7	42.04	154.8	121.8	31.96
n = 200	94242	2699	248.5	350.5	233.2	167.3
n = 500	904607	16650	2045	697.6	622.7	1068
$\delta = 0.50$						
n = 100	7756	276.9	39.92	21.28	43.63	28.26
n = 200	67537	626.0	121.3	71.90	37.84	73.39
n = 500	232434	2798	328.5	54.19	76.45	164.3
$\delta = 1.0$						
n = 100	49970	636.9	108.1	56.79	88.51	84.17
n = 200	247379	2345	281.7	131.5	111.5	176.2
n = 500	1188079	13853	1071	325.5	364.9	531.2

Table 2(a): Relative Efficiency of the LS estimates of the Slope Coefficient of Exogenous Covariate $\hat{\delta}_2$ (Endogeneity in the threshold alone)

Quantiles	MSE_{TR} / MSE_{THRET}			$MSE_{NAIVE} / MSE_{THRET}$		
	0.05	0.50	0.95	0.05	0.50	0.95
$\delta = 0.01$						
n = 100	1.713	2.182	5.736	1.301	4.998	16.06
n = 200	1.416	1.363	2.559	4.301	4.676	33.18
n = 500	2.165	1.432	1.531	13.05	7.151	75.22
$\delta = 0.05$						
n = 100	1.780	2.455	7.457	2.105	4.960	16.60
n = 200	1.556	1.481	4.298	3.766	4.701	31.43
n = 500	2.226	1.415	1.544	10.908	6.194	59.80
$\delta = 0.10$						
n = 100	2.123	2.691	10.36	1.614	4.236	14.30
n = 200	1.834	1.743	8.277	4.002	3.791	29.69
n = 500	2.331	1.545	1.771	5.682	3.764	25.32
$\delta = 0.25$						
n = 100	1.644	3.483	9.848	2.744	2.613	10.82
n = 200	3.244	2.619	7.732	2.313	2.074	5.593
n = 500	3.963	2.532	2.867	2.524	1.812	2.015
$\delta = 0.50$						
n = 100	1.724	2.548	2.761	2.018	1.601	1.481
n = 200	2.841	2.71	2.333	1.488	1.403	1.765
n = 500	7.758	3.702	2.789	4.257	1.726	1.733
$\delta = 1.0$						
n = 100	1.200	1.649	1.423	0.712	1.244	1.204
n = 200	1.434	2.168	2.066	1.530	1.509	1.513
n = 500	12.10	3.981	3.237	5.066	1.920	1.772

Table 2(b): Relative Efficiency of the GMM Estimates of the Slope Coefficient of Exogenous Covariate $\hat{\delta}_3$ (Endogeneity in both the threshold and the slope)

Quantiles	$MSE_{IVTR} / MSE_{THRETS}$			$MSE_{NAIVE} / MSE_{THRETS}$		
	0.05	0.50	0.95	0.05	0.50	0.95
$\delta = 0.01$						
n = 100	2.114	1.758	2.023	49.84	21.87	25.30
n = 200	1.739	1.459	1.510	27.32	27.32	28.93
n = 500	1.896	1.463	1.327	18.94	22.75	30.15
$\delta = 0.05$						
n = 100	2.555	1.782	2.258	25.98	20.81	26.86
n = 200	1.676	1.477	1.759	18.88	23.78	29.95
n = 500	2.187	1.594	1.529	28.21	17.91	22.35
$\delta = 0.10$						
n = 100	2.276	1.653	2.112	25.19	17.72	20.09
n = 200	3.079	1.564	2.029	17.23	18.91	19.72
n = 500	2.008	1.608	1.590	11.58	11.40	14.64
$\delta = 0.25$						
n = 100	2.077	1.603	1.958	12.53	12.16	14.25
n = 200	1.927	1.712	1.734	14.48	12.57	11.42
n = 500	2.400	1.607	1.770	9.173	8.474	10.49
$\delta = 0.50$						
n = 100	2.294	1.508	1.988	17.518	10.52	11.74
n = 200	0.794	2.093	1.811	9.817	11.56	11.71
n = 500	3.031	2.743	2.405	10.20	7.856	10.05
$\delta = 1.0$						
n = 100	2.649	2.857	2.585	20.35	17.57	16.11
n = 200	4.032	4.132	3.338	7.165	12.57	15.39
n = 500	19.07	8.875	4.877	9.201	11.09	12.86

Table 3: Relative Efficiency of the GMM Estimates of the Slope Coefficient of Endogenous Covariate $\hat{\delta}_2$

Quantiles	$MSE_{IVTR} / MSE_{THRETS}$			$MSE_{NAIVE} / MSE_{THRETS}$		
	0.05	0.50	0.95	0.05	0.50	0.95
$\delta = 0.01$						
n = 100	440.8	337.9	179.4	4924	1671.2	3784
n = 200	3508	703.2	269.2	10816	2004	4654
n = 500	43847	1965	443.6	17849	2123	5150
$\delta = 0.05$						
n = 100	326.1	312.8	175.8	4559	1567	3027
n = 200	1009	612.0	270.6	6998	1710	3629
n = 500	2935	1845	450.9	4844	1288	2365
$\delta = 0.10$						
n = 100	296.3	236.1	171.8	3430	1327	2369
n = 200	315.9	296.8	266.4	4913	1112	2402
n = 500	305.2	397.7	435.8	1267	650.3	623.5
$\delta = 0.25$						
n = 100	157.4	114.7	126.7	517.3	650.3	710.7
n = 200	126.6	126.1	129.0	362.1	402.0	414.8
n = 500	124.8	133.2	104.8	265.0	221.8	305.2
$\delta = 0.50$						
n = 100	268.1	151.9	99.06	402.9	389.4	484.2
n = 200	306.8	235.9	132.0	201.1	265.6	446.0
n = 500	1441	495.5	208.9	450.3	324.7	399.3
$\delta = 1.0$						
n = 100	755.1	473.1	215.6	258.8	569.1	809.8
n = 200	3581	1039	362.1	669.3	616.6	780.2
n = 500	101211	2608	657.4	14470	1863	833.2

Table 4♦: Regressions of log GDP per capita in 1995

	Linear Regression (2SLS)	THRETS (GMM)		Linear Regression (2SLS)	THRETS (GMM)		Linear Regression (2SLS)	THRETS (GMM)	
		<i>Avg. Expr.Risk ≤ 0.515</i>	<i>Avg. Expr.Risk > 0.515</i>		<i>Avg. Expr.Risk ≤ 0.515</i>	<i>Avg. Expr.Risk > 0.515</i>		<i>Avg. Expr.Risk ≤ 0.547</i>	<i>Avg. Expr.Risk > 0.547</i>
		90% CI = [0.483, 0.769]			90% CI = [0.483, 0.652]			90% CI = [0.500, 0.720]	
<u>Dependent Variable:</u> log GDP per capita (PPP basis) in 1995	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Average Expropriation Risk 1985-95	7.697*** (2.197)	5.516 (6.311)	6.204*** (1.553)	7.656*** (2.103)	7.938 (7.113)	7.558*** (2.232)	6.684** (2.841)	-6.998 (14.909)	8.570*** (2.838)
MALFAL94P	-1.277*** (0.365)	-0.726 (0.604)	-1.604*** (0.410)	-0.878* (0.460)	-0.943 (0.791)	-1.056** (0.450)	-0.876** (0.422)	0.204 (1.133)	-0.759 (0.485)
Ethnic Diversity	-	-	-	-0.872* (0.448)	0.176 (0.512)	-0.965** (0.443)	-0.831* (0.428)	-0.198 (0.383)	-1.156** (0.529)
Openness	-	-	-	-	-	-	0.504 (0.619)	2.158** (0.991)	-0.401 (0.966)
No. of observations	60	14	46	60	14	46	60	17	43

♦ All the regressions include a constant. Robust standard errors are in parentheses. “***” denotes significance at 1%, “**” at 5%, and “*” at 10%. The Average Expropriation Risk variable defers from Acemoglu, Johnson, and Robinson (2001) only in that it has been rescaled to take values from 0 to 1, with a higher score indicating higher less risk of expropriation. The lowest score for expropriation risk was 0.355 (Haiti) and the highest 1 (United States). We follow Acemoglu, Johnson, and Robinson (2001) and instrument for average expropriation risk using log settler mortality.